HARRISON COLLEGE INTERNAL EXAMINATION MARCH 2021 CARIBBEAN ADVANCED PROFICIENCY EXAMINATION SCHOOL BASED ASSESSMENT PURE MATHEMATICS PREVIEW UNIT I – TEST 1 1 hour 20 minutes

This examination paper consists of **8** printed pages and $\frac{2}{2}$ blank pages for extra working. This paper consists of **9** questions.

The maximum mark for this examination is **60**.

INSTRUCTIONS TO CANDIDATES

- (i) Write your NAME and FORM clearly in the spaces provided above
- (ii) Answer ALL questions in the SPACES PROVIDED
- (iii) DO NOT write your solutions to different questions beside each other
- (iv) Unless otherwise stated in the question, any numerical answer that is not <u>exact</u>, **MUST** be written correct to <u>three</u> (3) significant figures

EXAMINATION MATERIALS ALLOWED

- (a) Mathematical formulae
- (b) Scientific calculator (non-programmable, non-graphical)
- 1) Given that p and q are propositions, use the <u>algebra of propositions</u> to simplify fully $\sim (p \lor q) \lor (\sim p \land q)$ Ans. $\sim p$ [4]

2) Prove that for all $x \in \mathbf{R}$, $y \in \mathbf{R}$; $x^2 + y^2 \ge -2xy$ [4]

3) Without the use of a calculator, find the <u>EXACT</u> value of $\frac{\sqrt{7} - \sqrt{2}}{\sqrt{7} + \sqrt{2}} - \frac{\sqrt{7} + \sqrt{2}}{\sqrt{7} - \sqrt{2}}$. Ans. $-\frac{4\sqrt{14}}{5}$ [5]

4) Prove by mathematical induction that $9^{2n} - 1$ is a multiple of 8.

[7]

- **5**) The expression $f(x) \equiv x^3 bx + 6$ is exactly divisible by (x 2)
 - (i) Calculate the value of *b*. **Ans.** 7 [3]
 - (ii) Solve f(x) = 0. Ans. 1, 2, -3 [4]

6) (a) Solve for x, $3log_8x - 5 = 2log_x 8$. Ans. $\frac{1}{2}$, 64 [6]

(b) Solve for x the following equation
$$9^x - 7(3^x) = 6$$
. Ans. $\frac{ln\left(\frac{7+\sqrt{73}}{2}\right)}{ln3}$ [4]

7) The number of mosquito larvae, *N*, found in a pond initially was 3 200.

The number of larvae after t days was found to be directly proportional to $\left(\frac{3}{2}\right)^t$.

Calculate estimates of

- (i) the number of larvae after 3 days Ans. 10 800
- (ii) the number of days for which the population is expected to exceed 16 000. **Ans.** 4 [5]

[3]

8) Find the range of values of x for which $\left|\frac{x+8}{x-4}\right| \le 5, x \ne 4$. Ans. $x \le 2, x \ge 7$ [6]

9) If α , β and γ are the roots of the equation $3x^3 - 4x^2 - 5x + 2 = 0$, find the equation with roots $\alpha - 1$, $\beta - 1$ and $\gamma - 1$. Ans. $3x^3 + 5x^2 - 4x - 4 = 0$ [9]