# HARRISON COLLEGE END OF YEAR EXAMINATION 2019 THIRD YEAR MATHEMATICS DURATION: 1 Hour and Fifty Minutes

# **GENERAL INSTRUCTIONS TO CANDIDATES**

# 1) ALL QUESTIONS ARE TO BE ANSWERED IN THE SPACES PROVIDED ON THIS QUESTION PAPER. THERE ARE TWO EXTRA PAGES AT THE END OF THIS PAPER FOR ADDITIONAL OR ROUGH WORKING.

- This Examination Paper consists of ELEVEN printed pages and TWO blank pages.
- 3) All **TWENTY-TWO** questions are to be attempted.
- **4)** Number your responses <u>carefully</u> and <u>identically</u> (including any associated parts) as they appear on the question paper.
- 5) Calculators are ALLOWED.
- 6) If a numerical answer cannot be given <u>exactly</u>, and the accuracy required is not specified in the question, then in the case of an angle it <u>must</u> be given correct to **one** (1) decimal place, in other cases it <u>must</u> be given correct to <u>three (3)</u> <u>significant figures</u>.
- 7) The maximum mark for this Examination is 90.
- 8) Write your NAME and FORM below.

NAME OF STUDENT:	

FORM: \_\_\_\_\_

## DO NOT TURN THIS PAGE UNTIL YOU ARE TOLD TO DO SO

### LIST OF FORMULAE

Volume of Prism	V = Ah where A is the area of a cross-section and h is the perpendicular length.
Volume of Cylinder	$V = \pi r^2 h$ where <i>r</i> is the radius of the base and <i>h</i> is the perpendicular height.
Volume of a right pyramid	$V = \frac{1}{3}Ah$ where A is the area of the base and h is the perpendicular height.
Circumference	$C = 2\pi r$ where <i>r</i> is the radius of the circle.
Arc length	$S = \frac{\theta}{360} \times 2\pi r$ where $\theta$ is the angle subtended by the arc, measured in degrees.
Area of a circle	$A = \pi r^2$ where <i>r</i> is the radius of the circle.
Area of a sector	$A = \frac{\theta}{360} \times \pi r^2$ where $\theta$ is the angle of the sector, measured in degrees.
Area of Trapezium	$A = \frac{1}{2}(a+b)h$ where <i>a</i> and <i>b</i> are the lengths of the parallel sides and <i>h</i> is the perpendicular distance between the parallel sides.

Trigonometric ratios 
$$\sin \theta = \frac{opposite \ side}{hypotenuse}$$
  
 $\cos \theta = \frac{adjacent \ side}{hypotenuse}$   
 $\tan \theta = \frac{opposite \ side}{adjacent \ side}$ 
Opposite Adjacent

Area of a triangle Area of  $\Delta ABC = \frac{1}{2}bh$  where b is the length of the base and h is the perpendicular height. B

Area of 
$$\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$$
  $C \xrightarrow{a} b \xrightarrow{b} A$   
where  $s = \frac{a+b+c}{2}$ 

#### **SECTION I**

#### <u>**CIRCLE</u>** the **LETTER** that matches your response for Questions 1) to 10).</u>

1) If x \* y is defined to be  $x \div 2y$ , then -3 \* a

(A) 
$$-3 \div 2a$$
 (B)  $2a \div (-3)$  (C)  $3 \div 2a$  (D)  $-3 \div a$ 

2)

2



The diagram above illustrates the graph of

(A) 
$$y = 3x - 2$$
 (B)  $y = -2x + 3$  (C)  $y = \frac{3}{2}x - 3$  (D)  $y = \frac{3}{2}x + 3$ 

**3**) The gradient of the line parallel to 3x - 2y = 1 is

(A) 
$$\frac{2}{3}$$
 (B)  $\frac{3}{2}$  (C)  $-\frac{3}{2}$  (D)  $\frac{1}{2}$   
4) If  $\frac{2}{a+b} = \frac{1}{3}$ , then the value of  $\frac{a+b}{4}$  is  
(A)  $\frac{1}{12}$  (B)  $\frac{4}{3}$  (C)  $\frac{3}{2}$  (D) 12  
5) A number, 2*p*, is squared, then increase by 4. Algebraically, this may be represen

nted as resei ep

(A) 
$$2p^2 + 4$$
 (B)  $(2p+4)^2$  (C)  $4p+4$  (D)  $4(p^2+1)$ 

6) If 
$$\frac{2}{p} + \frac{1}{q} = r$$
, then p equals  
(A)  $r - \frac{1}{q}$  (B)  $\frac{2q}{qr-1}$  (C)  $\frac{2}{qr}$  (D)  $\frac{qr}{2}$ 

Questions 7), 8) and 9) refer to the numbers below which represent the weights, to the nearest kilogram, of seven picture frames.

7) The modal weight of the picture frames, in kilograms, is

- 8) The median weight of the picture frames, in kilograms, is
  - **(A)** 20 **(B)** 27 **(C)** 15 **(D)** 42

<b>9</b> ) The range of the data is			
(A) 8	<b>(B)</b> 15	( <b>C</b> ) 27	

10)



The triangle *ABC* above is right-angled at *B*. Angle  $ACB = 30^{\circ}$  and AC = 6 cm. The length of *AB*, in cm, is

 $(\mathbf{B})\frac{6}{\cos 30^0}$ 

**(A)** 6sin 30<sup>0</sup>

(C)  $\frac{6}{\tan 30^0}$  (D)  $\frac{6}{\tan 30^0}$ 

[Total: 10]

**(D)** 31

### **SECTION II**

# <u>All working MUST be clearly shown for Questions 11 – 22 in</u> the space provided after each Question

**11**) \$ 8 000 in savings bonds are invested for 3 years at the rate of 2 % per annum compounded interest. Calculate

(i) the value of the investment after one year.	[2]
(ii) the amount of interest received at the end of the invest	tment period. [3]

**12**) Simplify fully  $\left(k^{\frac{2}{3}}\right)^3 \times k^2$ .

**13**)  $\beta$  is directly proportional to the cube root of  $\alpha$ , and  $\beta = 5$  when  $\alpha = \frac{1}{8}$ . Using

# this information

- (i) Write an equation involving  $\beta$  and  $\alpha$ . [1]
- (ii) Calculate the value of  $\beta$  when  $\alpha = 27$ . [3]

<b>14)</b> (i)	r taken from y is at least 8. Write an inequality to represent this information.	[3]
(ii)	) Given that y is an integer, determine the least value of y when $r = \frac{4}{3}$	[3]

**15**) Solve for x and y, the simultaneous equations:  $\begin{aligned} 7x - 4y &= 37 \\ 6x + 3y &= 51 \end{aligned}$ 

[5]

16) (i) Find the equation of the straight line passing through the points (2, -3) and (0, -2). [2]
(ii) Determine the equation of the line passing through (4, 1) which is perpendicular to the line at (i) above. [3]

17) Jeff is married with three children in school. In the year 2018, he earned a gross income of \$ 50 000.

Tax-Free Allowances per year
Personal Allowance: \$ 20 000
Each school-age child: \$ 1500. Maximum claim is 2 children.
Tax Rates
First \$ 10 000 of taxable income: 3 %
Remainder: 5.5 %

Using the information in the table above, calculate

(i)	his total tax-free allowances	[3]
(ii)	his taxable income	[1]
(iii)	the amount of income tax paid	[5]
(iv)	his net income.	[2]

- **18)** An entrepreneur makes three sizes of bouquets; small, medium and large. Each bouquet contains roses, lilies and tulips. The table below shows some information about the number of bouquets made in one week.
  - (a) Complete the table below.

	Small	Medium	Large	TOTAL
Roses	7			23
Lilies		16		34
Tulips	3	8	2	
TOTAL	20		14	

#### Write your responses to part (b) in the space provided at the top of the next page.

- (b) One of the bouquets is selected at random. Determine the probability that the bouquet
  - (i) is medium
  - (ii) is made from tulips
  - (iii) is large and made from lilies
  - (iv) is small given that it is made from roses
  - (v) is made from roses given that it is medium

[7]

[5]

19)	A group	of students	each recor	rded the	distance	they t	ravelled	daily to	reach	school.
	The dista	ance, to the	nearest kil	ometre,	is record	ed bel	ow:			

Distance in kilometres	Frequency
1 - 5	5
6 - 10	2
11 - 15	4
16 - 20	8
21 - 25	3
26 - 30	3

- (i) State the modal class.
- (ii) Calculate the mean distance travelled.

[1] [8] 20) The figure below, not drawn to scale, represents a bird cage in the form of a cylinder surmounted by a cone. The diameter of the cylinder is 35 cm and its height is 25 cm. The total volume of the cage is 31 178 cm<sup>3</sup>.



Using  $\pi = \frac{22}{7}$ , calculate the total height of the cage

[5]

21) The diagram below, not drawn to scale, shows the sector of a circle OABC.

OA = 7 cm, AC = 8.03 cm and angle  $AOC = 70^{\circ}$ .







- 22) A man 1.5 metres tall is standing at a point *A* on the horizontal ground. His feet are 10 metres away from the base, *B*, of a cell phone tower, *BT*, which is 18 metres high.
  (i) Sketch a <u>fully labelled</u> diagram to show <u>ALL</u> of the above information. [6]
  - (ii) Calculate an estimate of the angle of elevation of the top, *T*, of the tower from his eyes.

[3]

**End of Examination**