THIRD FORM MATHEMATICS
P. CADOGAN

Promotion Examination 2009

Harrison College

Time $1 \frac{3}{4}$ hours

## INSTRUCTIONS

This question paper consists of FOUR printed pages.
Write your name clearly on EACH sheet of paper used.
Number your answers carefully and do NOT do questions beside one another.
All of the questions are to be attempted.
Calculators are allowed.
Write on your foolscap the LETTER that matches your response for Questions 1 - 10 .
All working MUST be shown for questions $11-18$.
Graph paper is available if required.
If a numerical answer cannot be given exactly, and the accuracy required is not specified in the question, then in the case of an angle it should be given to the nearest degree, in other cases it should be given correct to three (3) significant figures.

1. The result of $\frac{a^{2}(a+b)}{a}$ is
(A) $a^{2}(1+b)$
(B) $a^{2}\left(a^{2}+b\right)$
(C) $a(a+b)$.
(D) $a^{3}(a+b)$
2. The value of the expression $(p q r)^{2}$ when $p=2, q=-I$ and $r=\frac{1}{2}$ is:
(A) 1
(B) -1
(C) 4
(D) 2
3. $(-2 y)$ subtracted from $(-3 y)$ is:
(A) $-5 y$
B) $-y$
(C) $y$
(D) $6 y^{2}$
4. Given that $k$ is a constant, and that $m$ is inversely proportional to $n$ then
(A) $m=n$
(B) $m=k n$
(C) $n=k$
(D) $m=\frac{k}{n}$
5. $E C \$ 1.00=B D S \$ 0.75$, so $B D S \$ 7.50=$
(A) EC $\$ 75.00$
(B) $E C \$ 10.00$
(C) $E C \$ 100.00$
(D) $E C \$ 7.50$
6. The simple interest on $\$ 200$, invested for 2 years at $2 \%$ per annum is:
(A) $\$ 4$
(B) $\$ 100$
(C) $\$ 8$
(D) $\$ 50$
7. Which one of the following sets of numbers represents a function.
(A) $(1,2),(2,3),(3,4),(4,5)$
(B) $(1,2),(1,4),(3,8),(5,12)$
(C) $(0,14),(2,6),(2,9),(4,6)$
(D) $(-6,-2),(-6,-4),(-2,5),(4,2)$
8. The volume of a cone is given by
(A) $4 \pi r^{2}$
(B) $\pi r^{2}$
(C) $\frac{3}{4} \pi r^{3}$
(D) $\frac{1}{3} \pi r^{2} h$
9. In the diagram below, the bearing of $A$ from $B$ is:

(A) $60^{\circ}$
(B) $240^{\circ}$
(C) $300^{\circ}$
(D) $120^{\circ}$
10. Which one of the following is NOT a measure of central tendency in Statistics.
(A) mean
(B) graph
(C) median
(D) mode
11. $p$ varies directly as $(t+1)^{3} \cdot p=16$ when $t=1$. Find $p$ when $t=3$.
12. Jane's car cost $\$ 40000$ new. It depreciates in value by $20 \%$ per year. Calculate the car's value after 2 years.
13. Jim's annual income for the year 2008 was $\$ 28500$. His tax-free allowances are shown in the table below.

Tax-Free Allowances

| Personal Allowance | $\$ 5000$ per year |
| :---: | :---: |
| Utilities Allowance | $5 \%$ of Annual Income |

Calculate for income year 2008
a) (i) Jim's TOTAL tax-free allowances.
(ii) Jim's TAXABLE income.
b) A $8 \%$ tax is charged on the FIRST $\$ 20000$ of TAXABLE INCOME.

A $12 \%$ tax is charged on the portion of taxable income ABOVE $\$ 20000$. Calculate the TOTAL amount of income tax Jim pays.
14. The figure below (not drawn to scale) shows a straight line passing through the points $P$ and $Q$.

i) Write down the coordinates of the points $P$ and $Q$.

Find, by calculation, the
ii) length of the line segment $P Q$.
iii) mid-point of the line segment $P Q$.
iv) gradient of the line segment $P Q$.
v) equation of the perpendicular line that passes through the mid-point of the line segment $P Q$.
15. Solve the simultaneous equations

$$
5 x-3 y=18
$$

$$
\begin{equation*}
3 x+2 y=7 \tag{8}
\end{equation*}
$$

16. The curved surface area of the sphere below is $616 \mathrm{~cm}^{3}$.


Taking $\pi=\frac{22}{7}$, calculate EXACTLY the
i) radius of the sphere
ii) volume of the sphere.

NOTE: For a sphere
$V$ olume $=\frac{4}{3} \pi r^{3}$
Curved Surface Area $=4 \pi r^{2}$
17. The weights of a group of students in Form 3 are shown in the table below.

| Weight $(\mathrm{kg})$ | Frequency $(\boldsymbol{f})$ |
| :---: | :---: |
| $25-34$ | 7 |
| $35-44$ | 23 |
| $45-54$ | 39 |
| $55-64$ | 23 |
| $65-74$ | 18 |

i) How many students are in the group?
ii) State the modal class.
iii) By finding the mid-interval value, calculate the mean weight of the students.
iv) Calculate the probability that a student chosen at random weighs AT MOST 44 kg .
18. A vertical tower $T G$, of height 20 m stands on horizontal ground at $G$. From a point $H$, due EAST of $G$, the angle of elevation of $T$ is $25^{\circ}$.
i) Draw a clearly labelled diagram showing ALL the points, angles and distances.
ii) Calculate the distance TH.

