HARRISON COLLEGE PROMOTION EXAMINATIONS 2015: 4th Form

SOLUTIONS AND MARK SCHEME

1. A	6. A	11. C
2. B	7. C	12. B
3. C	8. B	13. D
4. D	9. B	14. A
5. B	10. C	15. C

Question	Working	Marks & comments
16.(i)	$ \begin{array}{c c} & & & \\ &$	$\left[\frac{1}{2}\right]$ mark for each subset correctly enumerated .]
(ii)	3x + 65 = 80	1 [for summing his terms from 16(i) AND equating to 80]
	<i>x</i> = 5	1 [correct answer only] 2
(iii)	$n(s \cap (w \cup C)) = 11 + 8 + 15 = 34$	1 [for summing his terms from appropriate subsets] 1
17. (i)	10xy - 8x - 15ny + 12n = 2x(5y - 4) - 3n(5y - 4) = (5y - 4)(2x - 3n)	1 [c.a.o] 1 [c.a.o] 2
(ii)	$5x^{2} - 125$ = 5(x ² - 25) = 5(x - 5)(x + 5)	1 1[correct answer only] 2
(iii)	$2x^2 - 9x - 5 = (2x + 1)(x - 5)$	2 2

18.(i)	$2x^2 - 6x + 3 = 0$	
	$x = \frac{6 \pm \sqrt{6^2 - 4(2)(3)}}{2(2)}$	1 [use of quadratic formula]
	$x = \frac{6 \pm \sqrt{12}}{4}$	1 [maximum of 2 marks for correct use of his expression]
	x = 0.63	1 [c.a.o]
	x = 2.37	1 [c.a.o] 4
(ii)	y = 20 - 3x	
	$y = 2x^2$	
	$2x^2 = 20 - 3x$	1 equating expressions
	$2x^2 + 3x - 20 = 0$	
	$2x^{2} + 3x - 20 = 0$ (2x - 5)(x + 4) = 0	1 factorising
	$x = \frac{5}{2} \qquad x = -4$ $y = \frac{25}{2} \qquad y = 32$	1 correct values of x
	$y = \frac{25}{2} \qquad y = 32$	1 correct values of y 4

19(i))	$fg(2) = f(2^2 + 2 + 2) = f(8)$	1
	= 2 (8) + 3 = 19	1 2
(ii)(a)	$fg(x) = 2(x^2 + x + 2) + 3$	1
	$=2x^2+2x+7$	1 2
(ii)(b)	$f^{-1}(x) = \frac{x-3}{2}$	1 attempting to make "y" the subject. 1 c.a.o 2
		1 C.d.0 Z
(iii)	2(2x + 3) + 3 = 2x + 3 4x + 9 = 2x + 3 2x = -6	1 substituting 1 simplifying
	x = -3	1 c.a.o 3

20(a)	Bearing of C from B = $360 - 215 = 145^{\circ}$	1 1 [correct answer only] 2
(b)	$AC^2 = 40^2 + 60^2 - 2 \times 40 \times 60 \times \cos 115 =$	1 [for use of cosine rule] 1 for use of correct lengths and angle
	$AC^2 = 38.64$	1
	AC = 85.02	1 [correct evaluation of his expression] 4
(iii)	$\frac{\sin A}{60} = \frac{\sin 115}{85.02}$	1 [use of either sine or cosine rule correctly]
	$\sin A =$	1
	angle $A = 39.76^{\circ}$	1 [correct evaluation of his expression]
	Bearing of C from A = 80 + 39.76 = 119.8°	1 4
21.(i)	$\overline{OQ} = 3\mathbf{b} + 3\mathbf{a}$	1 1
	$\overline{OE} = \frac{2}{3}(3\boldsymbol{b} + \boldsymbol{3}\boldsymbol{a})$	1 1
	= 2a + 2b	
	$\overline{DE} = -\boldsymbol{a} + 2\boldsymbol{a} + 2\boldsymbol{b}$	
	= a + 2b	1 1
(ii)	$\overline{EF} = \boldsymbol{a} + 2\boldsymbol{b}$	
	$\overline{DE} = \overline{EF}$	1
	So DE and EF are parallel and since E is a common point D, E and F are collinear.	1 2